



MATHEMATICS CH-10- VECTORS

Name: _____

Date: _____

Class: XII Sec: ____

1. The scalar product of the vectors $i + j + k$ with a unit vector along the sum of the vectors $2i + 4j - 5k$ and $\lambda i + 2j + 3k$ is equal to 1. Find the value of λ .
2. If \mathbf{a} , \mathbf{b} , \mathbf{c} are three vectors such that $\mathbf{a} \times \mathbf{b} = \mathbf{c}$, $\mathbf{b} \times \mathbf{c} = \mathbf{a}$, prove that \mathbf{a} , \mathbf{b} , \mathbf{c} are mutually perpendicular with $|\mathbf{b}|=1$ and $|\mathbf{a}|=|\mathbf{c}|$.
3. The magnitude of the vector product of the vector $i + j + k$ with a unit vector along the sum of the vector $2i+4j-5k$ and $\lambda i+2j+3k$ is equal to $\sqrt{2}$. Find the value of λ .
4. Let $\mathbf{a} = i+4j+2k$, $\mathbf{b} = 3i-2j+7k$ and $\mathbf{c} = 2i-j+4k$. Find a vector \mathbf{d} which is perpendicular to both \mathbf{a} and \mathbf{b} and $\mathbf{c} \cdot \mathbf{d} = 15$.
5. If $\mathbf{a} \neq 0$, $\mathbf{a} \cdot \mathbf{b} = \mathbf{a} \cdot \mathbf{c}$ and $\mathbf{a} \times \mathbf{b} = \mathbf{a} \times \mathbf{c}$, then show that $\mathbf{b} = \mathbf{c}$.
6. Find λ when the projection of $\mathbf{a} = \lambda i + j + 4k$ on $\mathbf{b} = 2i + 6j + 3k$ is 4 units.
7. If $\mathbf{a} \times \mathbf{b} = \mathbf{c} \times \mathbf{d}$ and $\mathbf{a} \times \mathbf{c} = \mathbf{b} \times \mathbf{d}$, show that $\mathbf{a} - \mathbf{d}$ is parallel to $\mathbf{b} - \mathbf{c}$ where $\mathbf{a} \neq \mathbf{d}$ and $\mathbf{b} \neq \mathbf{c}$.
8. Find the direction cosines of the line which is perpendicular to the lines with direction cosines proportional to 1, -2, 2 and 0, 2, -1.
9. If $\mathbf{a} \times \mathbf{b} = \mathbf{c} \times \mathbf{d}$ and $\mathbf{a} \times \mathbf{c} = \mathbf{b} \times \mathbf{d}$, then show that $(\mathbf{a} - \mathbf{d})$ is parallel to $(\mathbf{b} - \mathbf{c})$, it is being given that $\mathbf{a} \neq \mathbf{d}$ and $\mathbf{b} \neq \mathbf{c}$.
10. If \mathbf{a} , \mathbf{b} , \mathbf{c} are three vectors such that $\mathbf{a} \cdot \mathbf{b} = \mathbf{a} \cdot \mathbf{c}$ and $\mathbf{a} \times \mathbf{b} = \mathbf{a} \times \mathbf{c}$, given $\mathbf{a} \neq 0$, then show that $\mathbf{b} = \mathbf{c}$.
11. If $\mathbf{a} + \mathbf{b} + \mathbf{c} = 0$ and $|\mathbf{a}| = 3$, $|\mathbf{b}| = 5$ and $|\mathbf{c}| = 7$, then show that the angle between \mathbf{a} and \mathbf{b} is 60° .
12. If $\mathbf{a} + \mathbf{b}$, $\mathbf{b} + \mathbf{c}$ and $\mathbf{c} + \mathbf{a}$ are coplanar, then show that the vectors \mathbf{a} , \mathbf{b} , \mathbf{c} are coplanar.